

## 6-5 THE COMPLEX PLANE

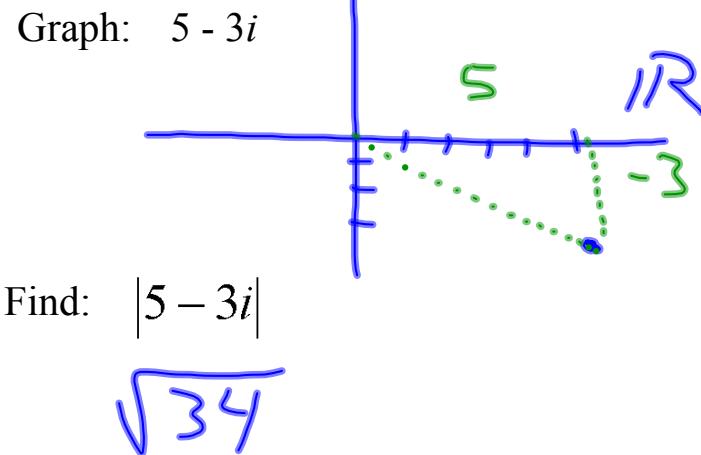
Complex number in standard form -

$$z = a + bi$$

Graph: 5



$$\text{Find: } |5| = 5$$

Graph:  $5 - 3i$ 

$$\text{Find: } |5 - 3i|$$

$$\sqrt{34}$$

Ex 1 Evaluate the following:

$$(5 - 3i) + (2 + 7i)$$

$$(5 - 3i) - (2 + 7i)$$

$$(5 - 3i)(2 + 7i)$$

$$10 + 35i - 6i - 21i^2$$

$$31 + 29i$$

$$(5 - 3i)^2$$

$$(5 - 3i)(5 - 3i)$$

$$(5 - 3i)(5 - 3i)$$

$$(5 - 3i)^3$$

$$(5 - 3i)^4$$

$$(5 - 3i)^5$$

Trigonometric (Polar) form of  $z = a + bi$

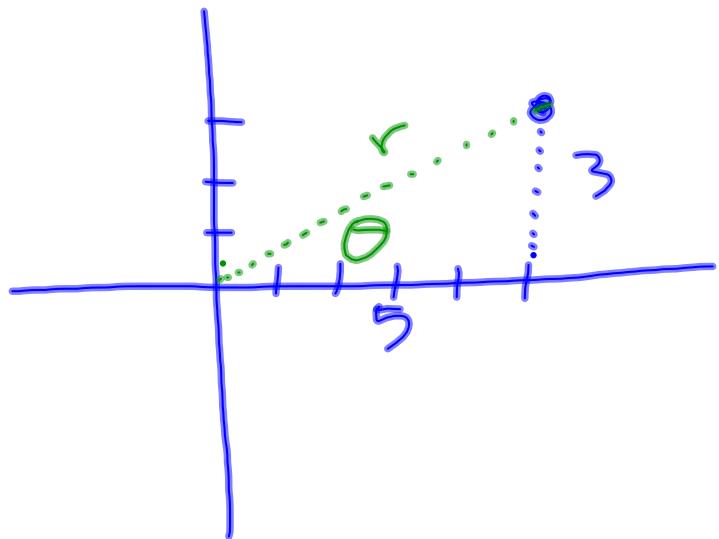
$$z = r(\cos \theta + i \sin \theta)$$

$$r = \sqrt{a^2 + b^2}$$

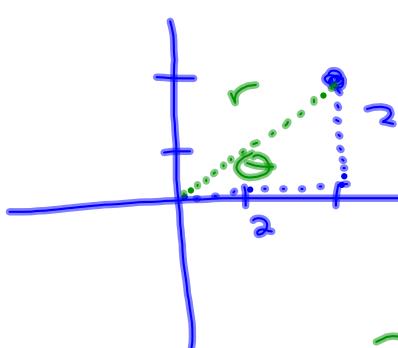
$$\tan \theta = \frac{b}{a}$$

$$a = r \cos \theta$$

$$b = r \sin \theta$$



Ex 2 Find the trigonometric (polar) form of  $2 + 2i$



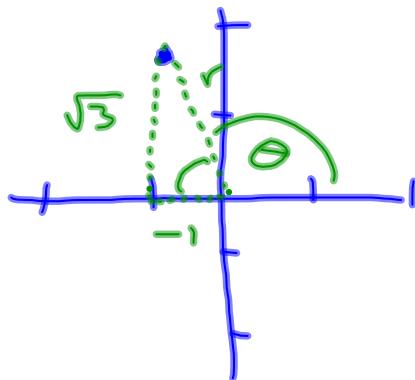
$$r = 2\sqrt{2}$$

$$\theta = 45^\circ$$

$$z = r(\cos \theta + i \sin \theta)$$

$$z = 2\sqrt{2} \left( \cos 45^\circ + i \sin 45^\circ \right)$$

Ex 3 Find the trigonometric (polar) form of  $-1 + \sqrt{3}i$

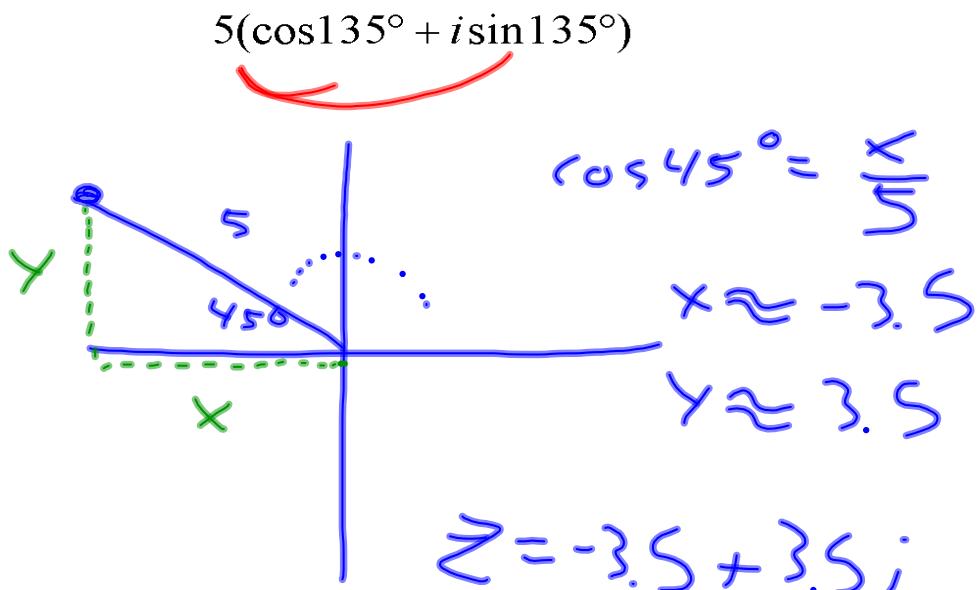


$$z = 2(\cos 120^\circ + i \sin 120^\circ)$$

$$r = 2$$

$$\tan \theta = \frac{\sqrt{3}}{-1}, \quad \theta = 120^\circ$$

Ex 4 Write the complex number in standard form.



Ex 5 Write the complex number in standard form.

$$4(\cos 60^\circ + i \sin 60^\circ)$$

2 + 3.5 i

Homework  
p.456  
#1-39 odds